

M-MACBETH:
A DECISION SUPPORT TOOL
FOR MULTI-CRITERIA
VALUE MEASUREMENT BASED ON
QUALITATIVE VALUE
JUDGEMENTS

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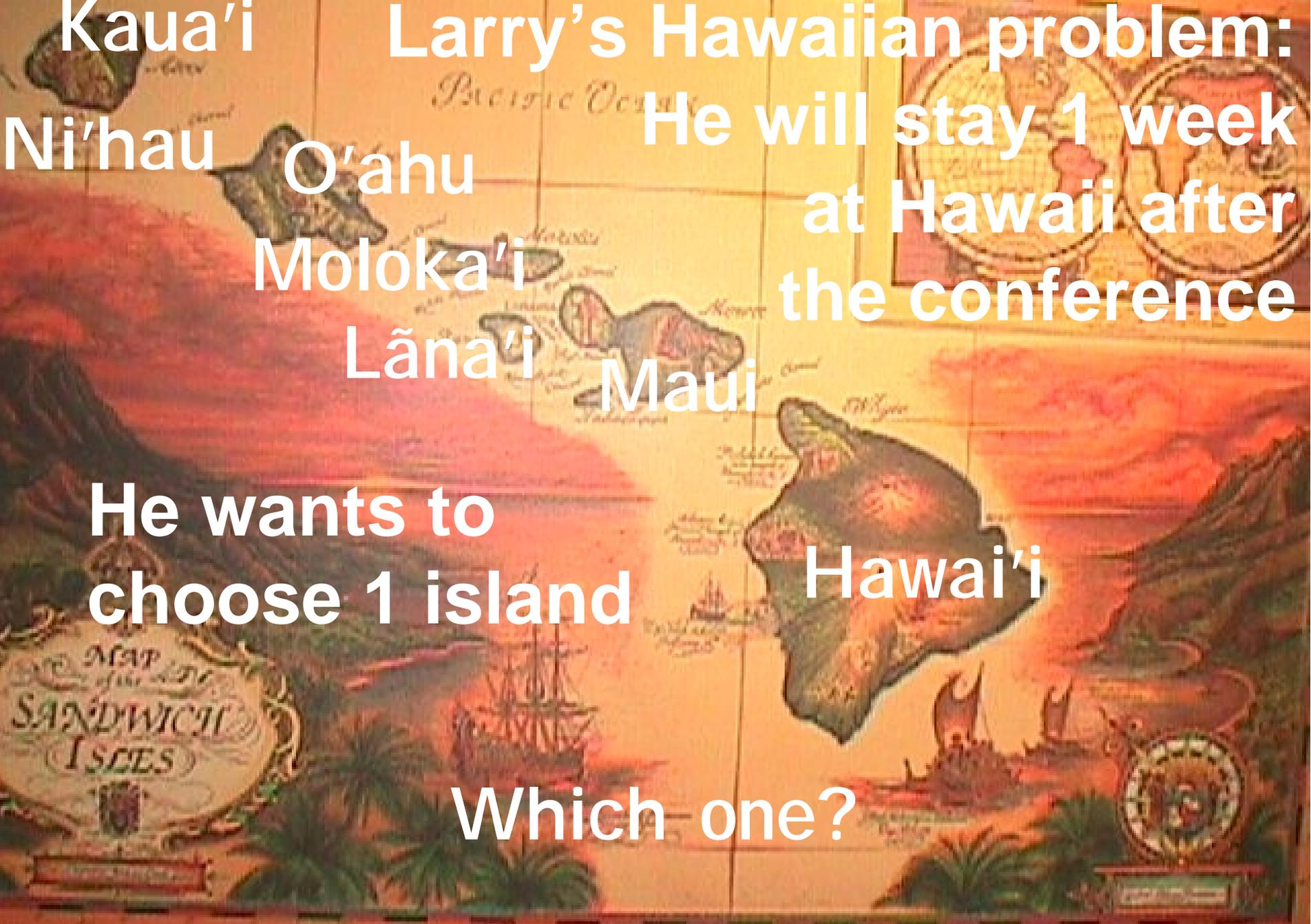
OUTLINE

- Overview of Multi-Criteria Value Measurement:
 - Measuring the relative value of options in each criterion:
Numerical and
non-numerical approaches (MACBETH)
 - Criteria weighting procedures

Slides available in: alfa.ist.utl.pt/~cbana/

- Demonstration of M-MACBETH

Download Trial version in: www.umh.ac.be/~smq/



Kaua'i

Larry's Hawaiian problem:

Ni'hou

He will stay 1 week
at Hawaii after
the conference

O'ahu

Moloka'i

Lāna'i

Maui

He wants to
choose 1 island

Hawai'i

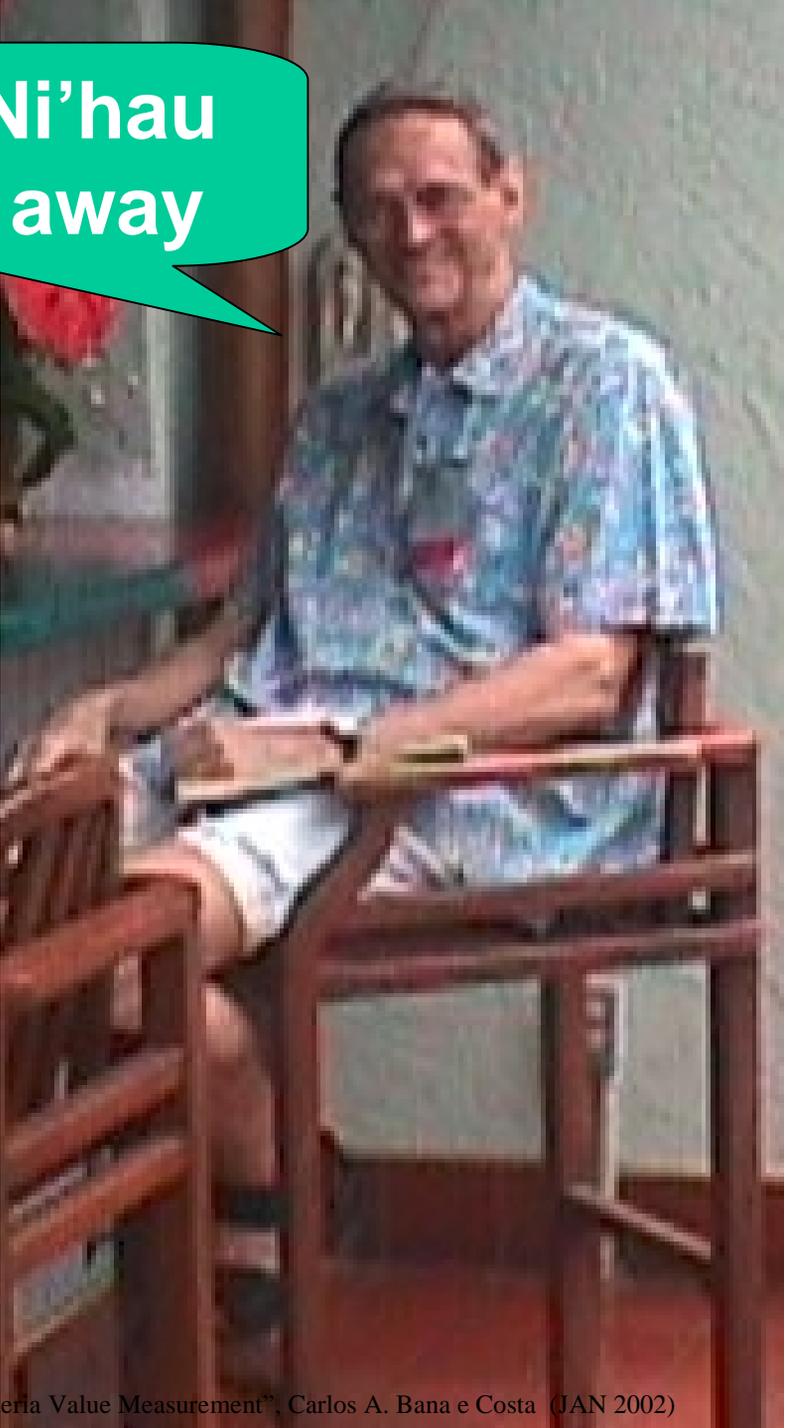
Which one?



I am in
the darkness!
Can you help me,
Carlos?

Define options: Screening

Kauha'i & Ni'hau
are too far away



New file

File name:

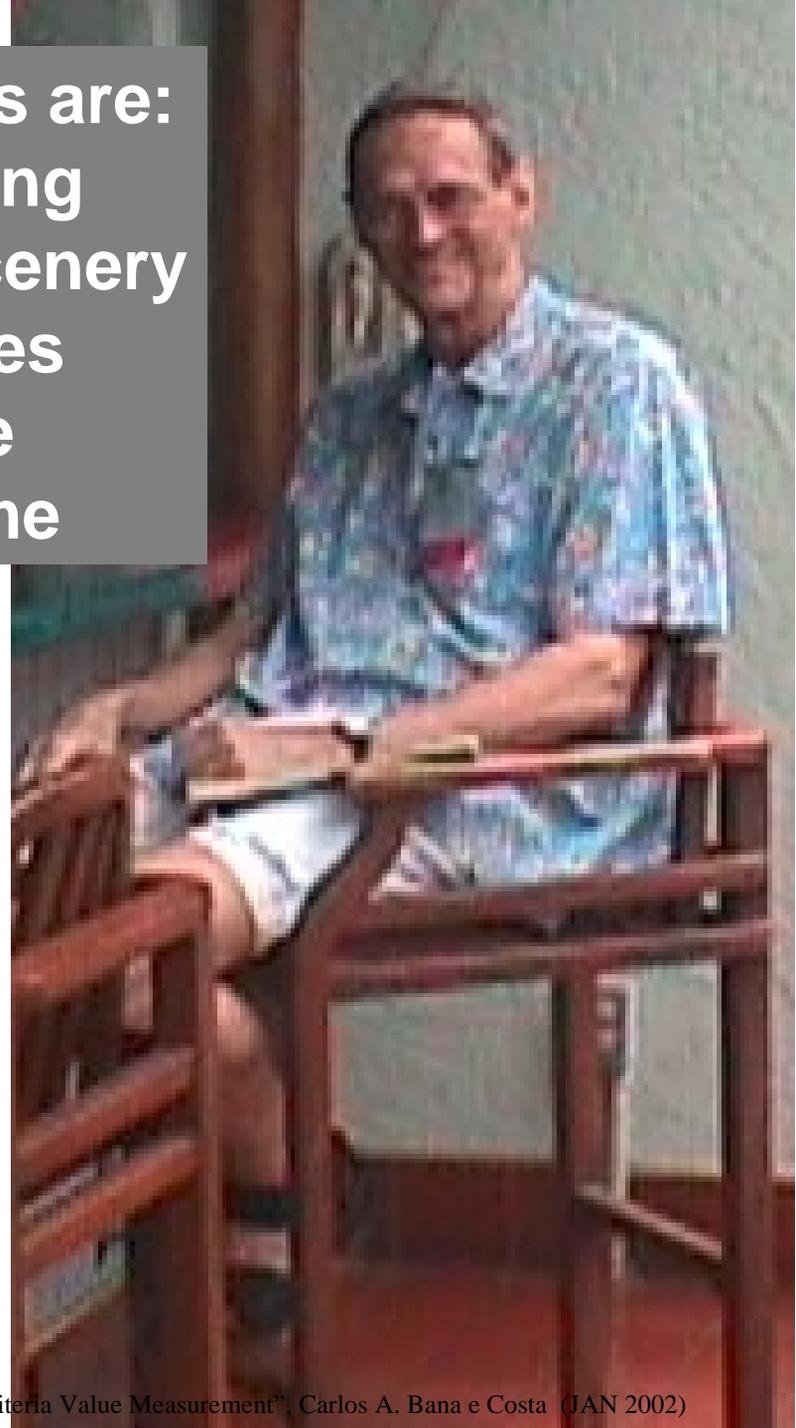
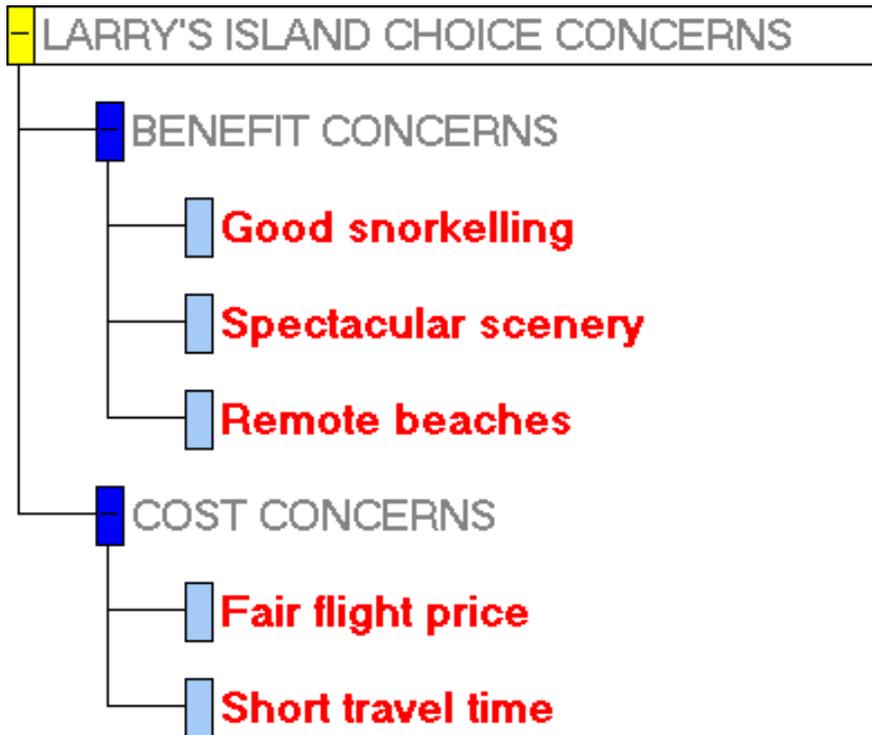
Actions

-	+	Names	Short
1		Oahu	Oahu
2		Molokai	Molo
3		Lanai	Lana
4		Maui	Maui
5		Hawaii (the big island)	Big

Define criteria

- My key concerns are:
- Good snorkelling
 - Spectacular scenery
 - Remote beaches
 - Fair flight price
 - Short travel time

Value tree



Evaluation framework: Additive value model

$$V(a) - V(b) = \sum_{j=1}^n k_j \cdot [v_j(a) - v_j(b)]$$

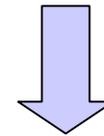
With:

$$\left\{ \begin{array}{l} v_j(\text{best}_j) = 100, \forall j \\ v_j(\text{worst}_j) = 0, \forall j \\ V(\text{best allover}) = 100 \\ V(\text{worst allover}) = 0 \end{array} \right.$$

$V(\bullet)$ overall value of option \bullet

$v_j(\bullet)$ partial value (score)
of option \bullet
in terms of criterion j

k_j scaling constant
(relative weight)
of criterion j



$$\sum_{j=1}^n k_j = 1 \quad \text{and} \quad k_j > 0 \quad (j = 1, \dots, n)$$

Scoring the options against each criterion:

**Techniques for cardinal (interval)
value measurement**

Numerical approaches

“**Direct rating,**

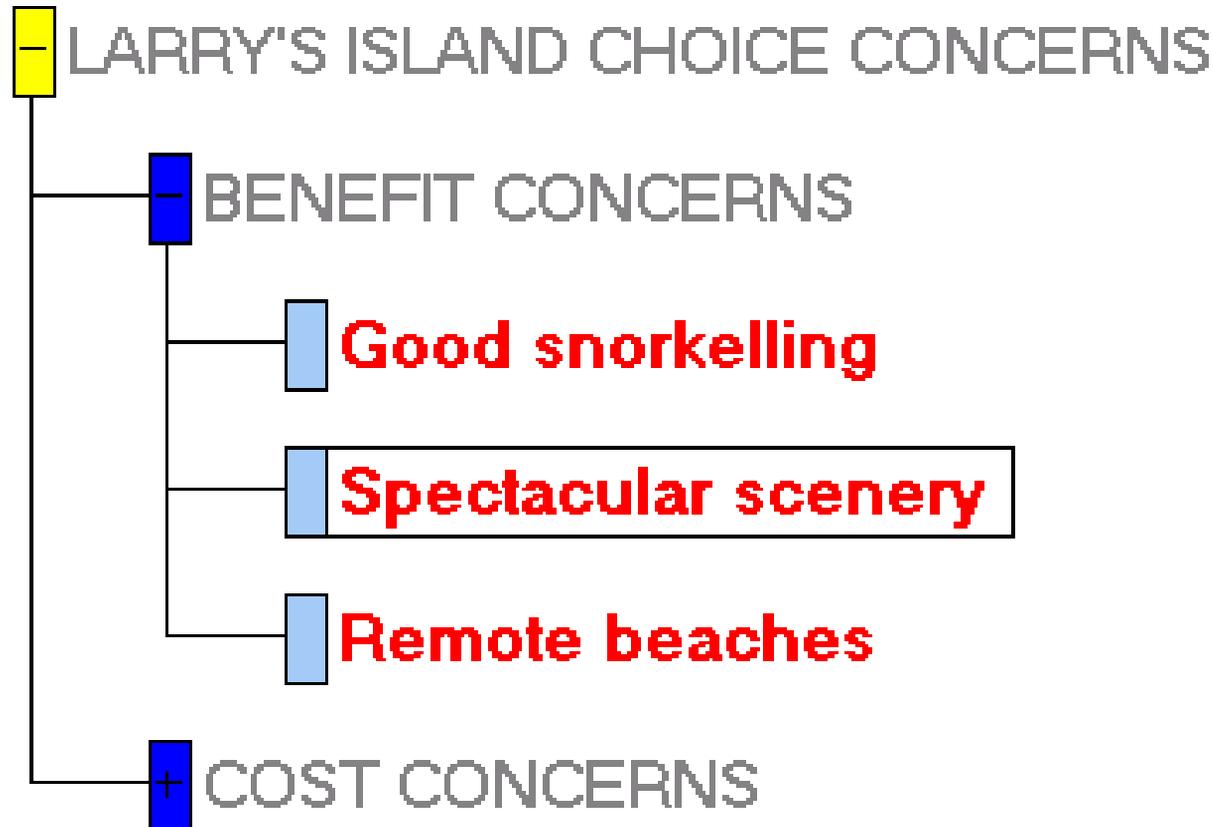
ratio estimation, category estimation, curve drawing

are versions of **numerical estimation methods**

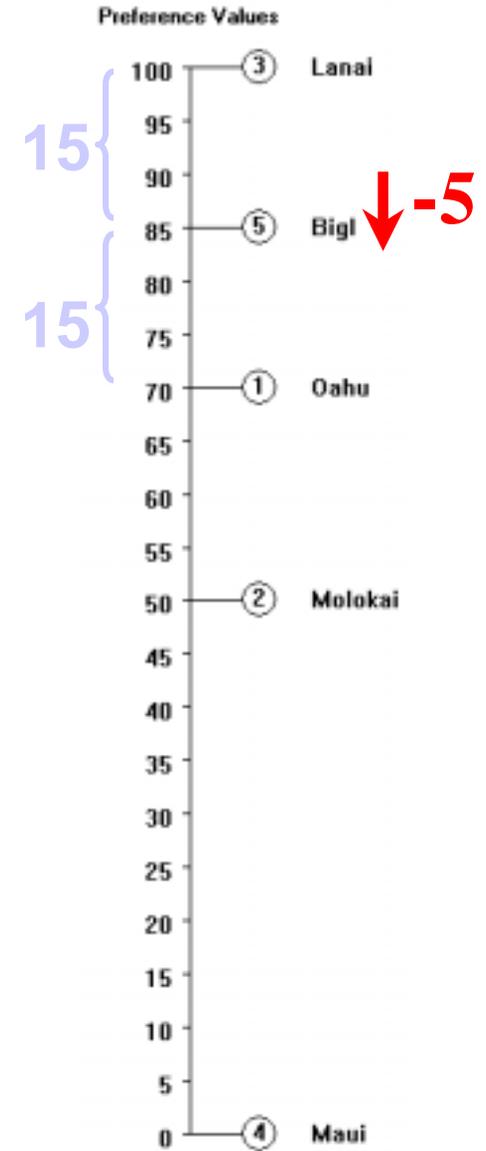
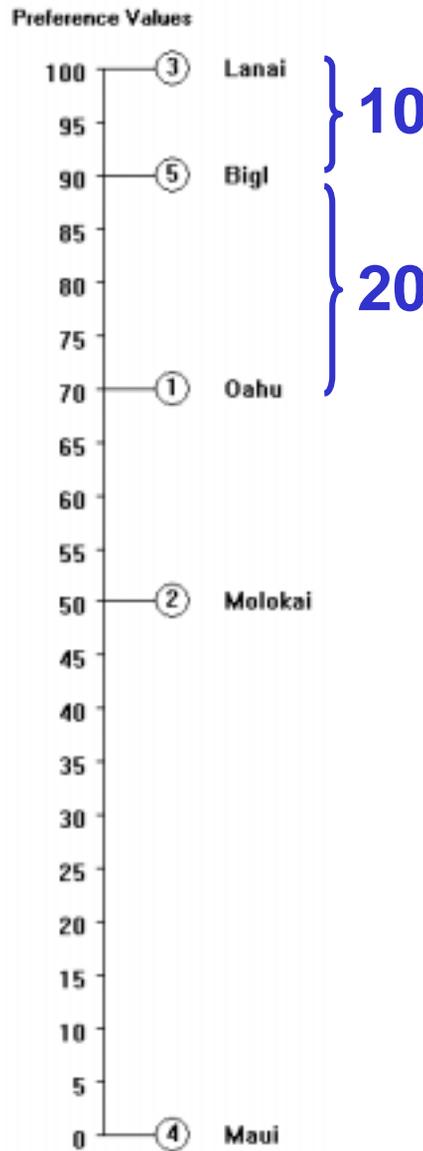
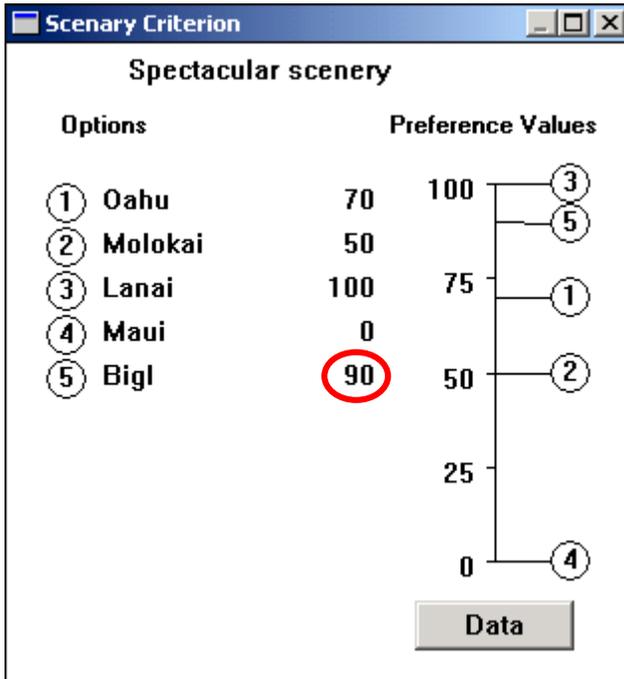
in which respondents are presented with some anchored scale and asked to rate or otherwise estimate numerically the attractiveness of the stimulus relative to the anchors.”

(von Winterfeldt & Edwards, 1986)

Example 1: Larry's "Spectacular scenery" concern

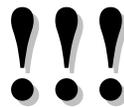


Direct Rating



$$[v(Bi) - v(Oa)] = 2.[v(La) - v(Bi)] \quad (90-70) = 2.(100-90)$$

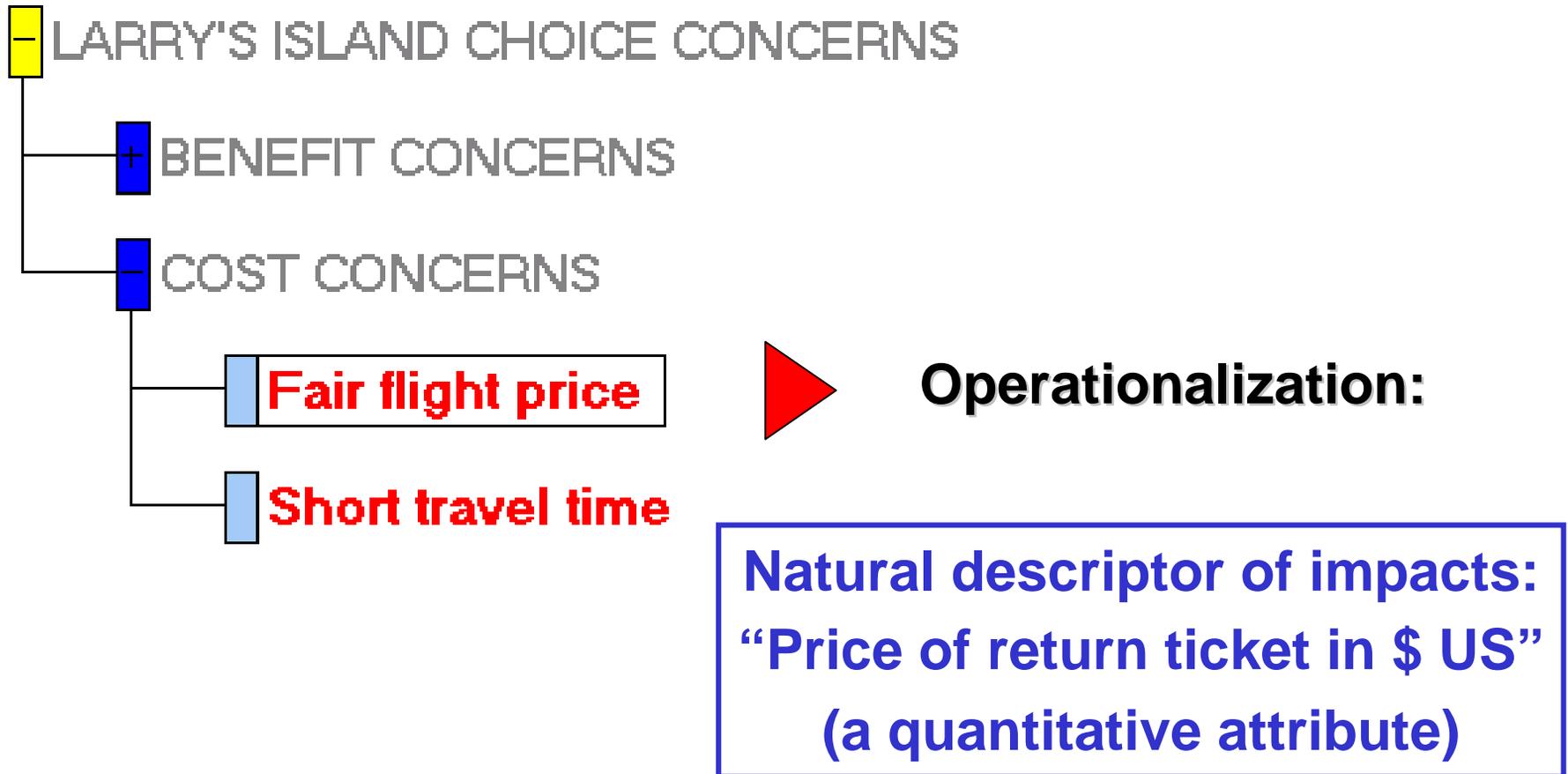
$$[v(Bi) - v(Oa)] = [v(La) - v(Bi)] \quad (85-70) = (100-85)$$



Building (interval) value functions

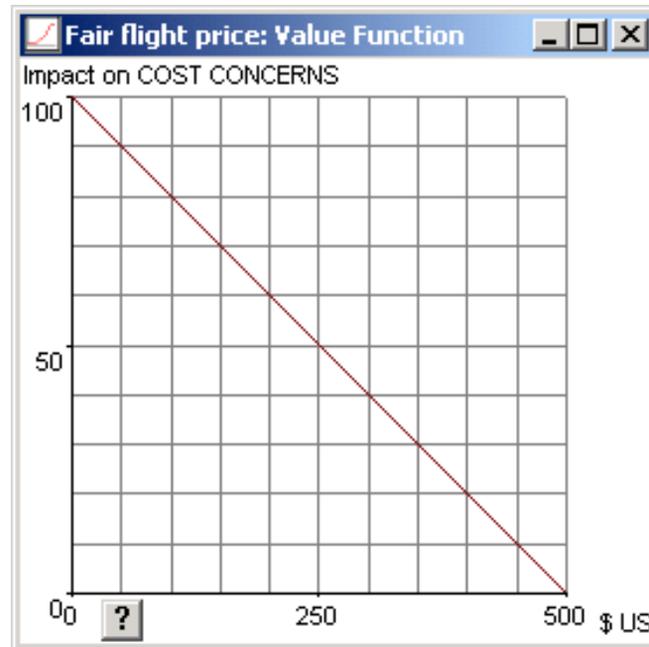
**a value function
enables to transform
impacts into scores**

Example 2: Larry's "Fair flight price" concern



Linear value function: Proportional scores

Common when the concern has a natural numerical descriptor



$$v_{\$} (?) = \frac{? - \text{least attractive cost}}{\text{most attractive cost} - \text{least attractive cost}} \times 100$$

Building (interval) value functions: “Bisection” or “mid-point splitting” approach

“In

bisection techniques

a most preferred stimulus and a least preferred stimulus are identified, and subsequently a midpoint stimulus is found that is equidistant from both extremes.”

(von Winterfeldt & Edwards, 1986)

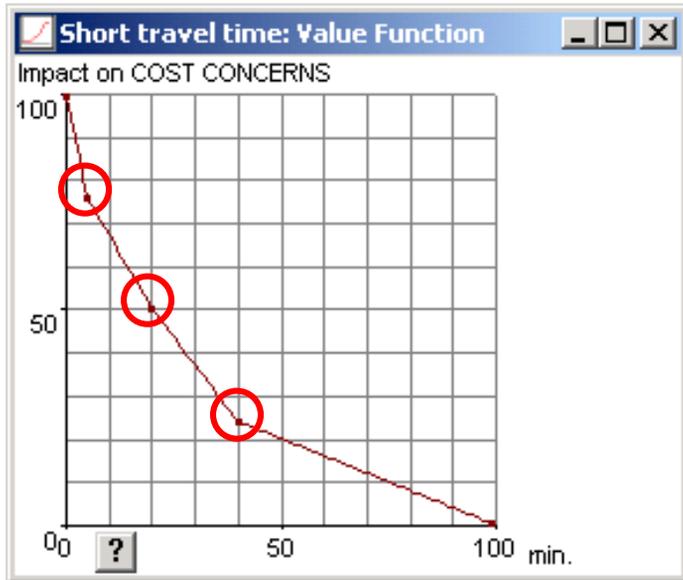
Example 3: Larry's "Short travel time" concern



Operationalization:

**Indirect descriptor of impacts:
"Travel time in minutes"
(a quantitative attribute)**

Non-linear value function: Bisection technique



Find ‘? min.’ so that
the difference in attractiveness between
‘0 min.’ and ‘? min.’
is equal to
the difference in attractiveness between
‘? min.’ and ‘100 min.’

$$v(0 \text{ min.}) - v(? \text{ min.}) = v(? \text{ min.}) - v(100 \text{ min.})$$

$$100 - v(20 \text{ min.}) = v(20 \text{ min.}) - 0$$
$$v(20 \text{ min.}) = 50$$

Similar questions to find
the midpoints 25 and 75

Piecewise linear value function or curve fitting

Non-numerical approaches: MACBETH

What to do when evaluators
do not feel comfortable
in directly scoring the options?

Use **MACBETH**
(**M**easuring **A**tractiveness by a
Categorical **B**ased
Evaluation **T**echnique)

**An interactive approach to guide the construction of an interval
value scale, based on qualitative value judgments**

How does it work?

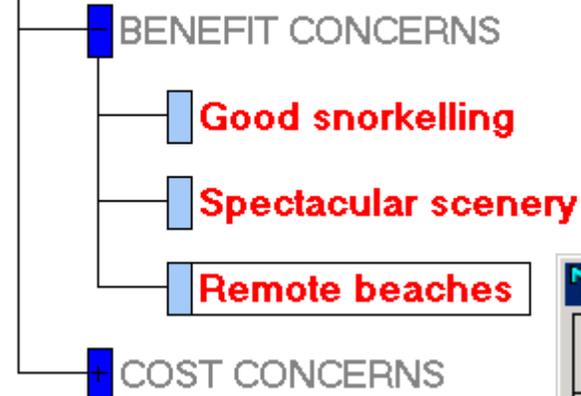
MACBETH uses a simple question-answer protocol which involves only two options in each question: Ask the evaluator to pair-wise compare options by given a *qualitative* judgement of the difference in attractiveness between each two options

**For x and y such that
x is preferred to y,
the difference in attractiveness
between x and y is:**

- very weak
- weak
- moderate
- strong
- v. strong
- extreme

Example 4: Larry's "Remote beaches" concern

LARRY'S ISLAND CHOICE CONCERNS



Remote beaches

	Bigl	Molo	Lana	Maui	Oahu
Bigl	no	weak-mod	moderate	strong	v. strong
Molo		no	↑ very weak	↓ strong	strong
Lana			no	moderate	↑ moderate
Maui				no	↓ weak
Oahu					no

extreme

v. strong

strong

moderate

weak

very weak

no

Inconsistent judgements

Suggestion 1 of 4 : 1 modification(s)

Interactive discussion of inconsistency

The screenshot displays a multi-criteria decision analysis (MCDA) software interface. It features several windows and a central criteria tree.

Remote beaches (Top Left): A comparison matrix for five islands: Bigl, Molo, Lana, Maui, and Oahu. The matrix shows pairwise comparisons using linguistic terms. A vertical legend on the right lists the terms: extreme, v. strong, strong, moderate, weak, very weak, and no.

	Bigl	Molo	Lana	Maui	Oahu
Bigl	no	weak-mod	moderate	strong	v. strong
Molo		no	very weak	strong	strong
Lana			no	moderate	moderate
Maui				no	weak
Oahu					

Inconsistent judgements (Middle Left): A red text box indicating "Inconsistent judgements" and "Suggestion 1 of 4 : 1 modification(s)".

Criteria (Center): A hierarchical tree titled "LARRY'S ISLAND CHOICE CONCERNS". The tree branches into "BENEFIT CONCERNS" and "COST CONCERNS". Under "BENEFIT CONCERNS", there are three sub-criteria: "Good snorkelling", "Spectacular scenery", and "Remote beaches". "Remote beaches" is highlighted with a red box.

Remote beaches (Bottom Left): A second comparison matrix, identical to the one in the top left, but with a vertical legend on the right that is partially obscured.

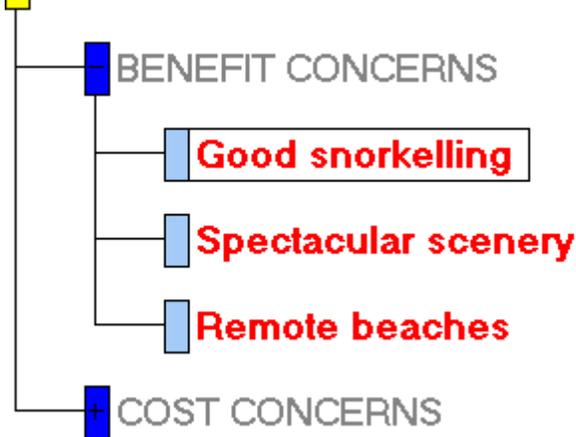
Consistent judgements (Bottom Left): A green text box indicating "Consistent judgements".

Remote beaches (Right): A vertical scale showing the relative importance of the islands based on the criteria. The values are: Bigl (100), Molo (70), Lana (50), Maui (10), and Oahu (0). The "Oahu" value is highlighted in green.

Qualitative descriptor

Example 5: Larry's "Good snorkelling" concern

LARRY'S ISLAND CHOICE CONCERNS



Operationalization:

**Qualitative descriptor of impacts
(constructed attribute):**

Descriptor levels :

-	+	Names	Short
1		Excellent snorkelling nearby hotel	ExcNear
2		Good snorkelling nearby hotel	GoodNear
3		Excellent snorkelling but out-of-the-way	ExcOut
4		Good snorkelling but out-of-the-way	GoodOut

Preference scale: MACBETH

Macbeth for MCDA : D:\TOSHIBA D\CONFER_VISITAS\MAUI 2001\LarrysHawaiianislandchoice3

File Actions Weighting Windows Options Help

200% bold

Criteria

- LARRY'S ISLAND CHOICE CONCERNS
 - BENEFIT CONCERNS
 - Good snorkelling
 - Spectacular scenery
 - Remote beaches
 - COST CONCERNS

Good snorkelling

	ExcNear	GoodNear	ExcOut	GoodOut	Current scale
ExcNear	no	strong	strg-vstr	extreme	100.00
GoodNear		no	weak	strong	60.00
ExcOut			no	strong	40.00
GoodOut				no	0.00

Consistent judgements

Good snorkelling

- ExcNear 100
- GoodNear 60
- ExcOut 40
- GoodOut 0

Weighting procedures:

TRADEOFF PROCEDURE

(Keeney & Raiffa, 1976)

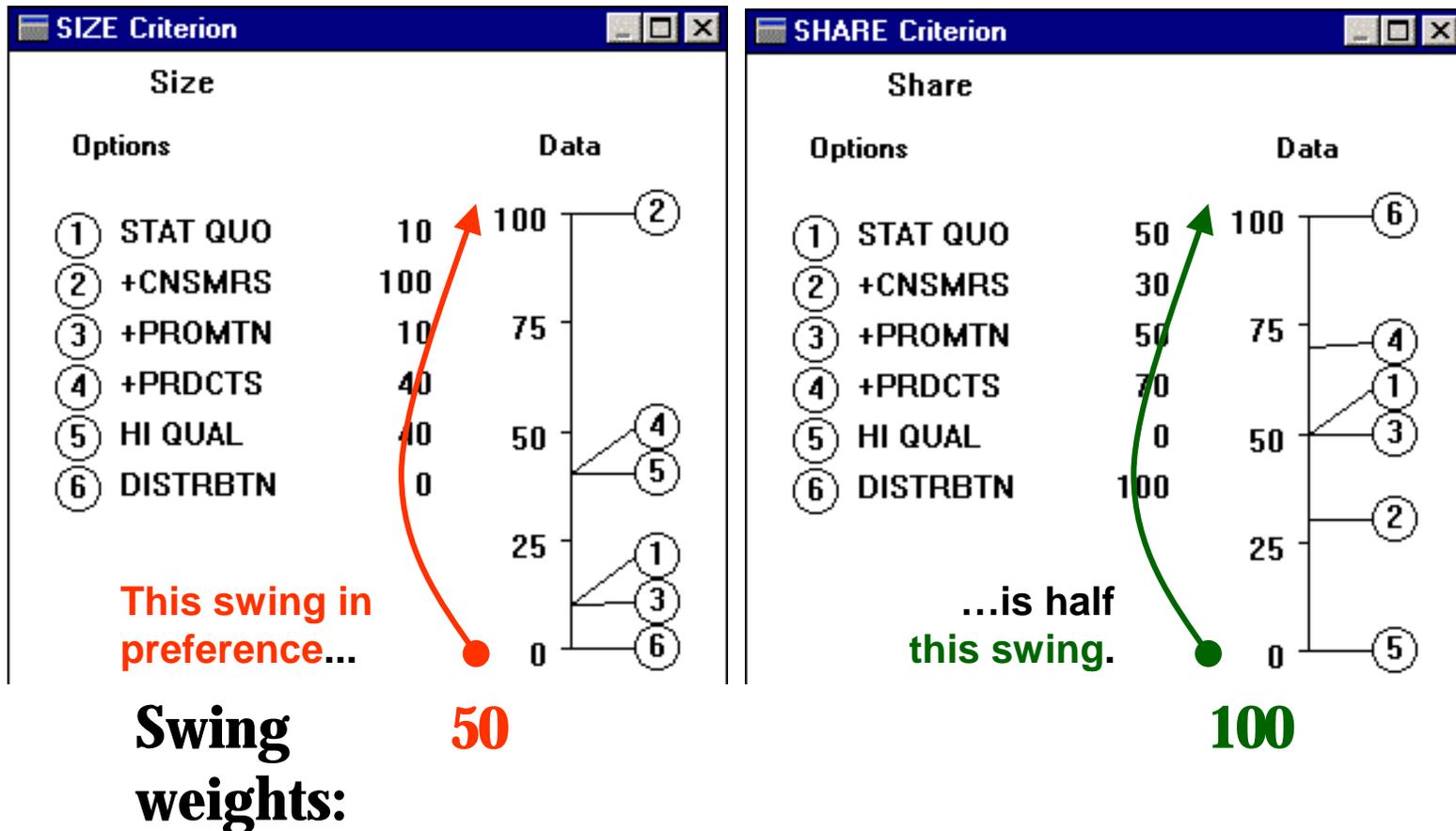
SWING WEIGHTING PROCEDURE

(von Winterfeldt & Edwards, 1986)

MACBETH

(Bana e Costa & Vansnick, 1997, 1999)

Swing weighting procedure



“How big is the difference, and how much do you care about it?”

SWING WEIGHTING PROCEDURE

The swing procedure starts from an alternative with the worst impacts in all the criteria

The evaluator is allowed to change from worst impact to best in one PV.

He or she is asked which 'swing' from worst to the best impact would result in the largest, second largest, etc., improvement of global attractiveness. The criterion with the most preferred swing is assigned 100 points.

The magnitudes of all other swings are expressed as percentages of the largest swing.

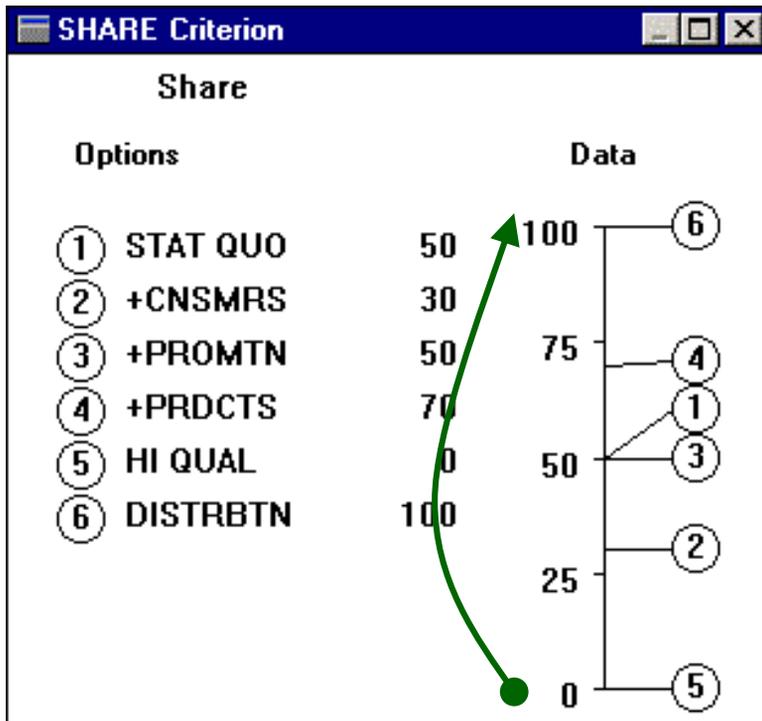
The derived percentages are the raw weights that are normalized to yield final weights.

(Adapted from Weber & Borchering, 1993.)

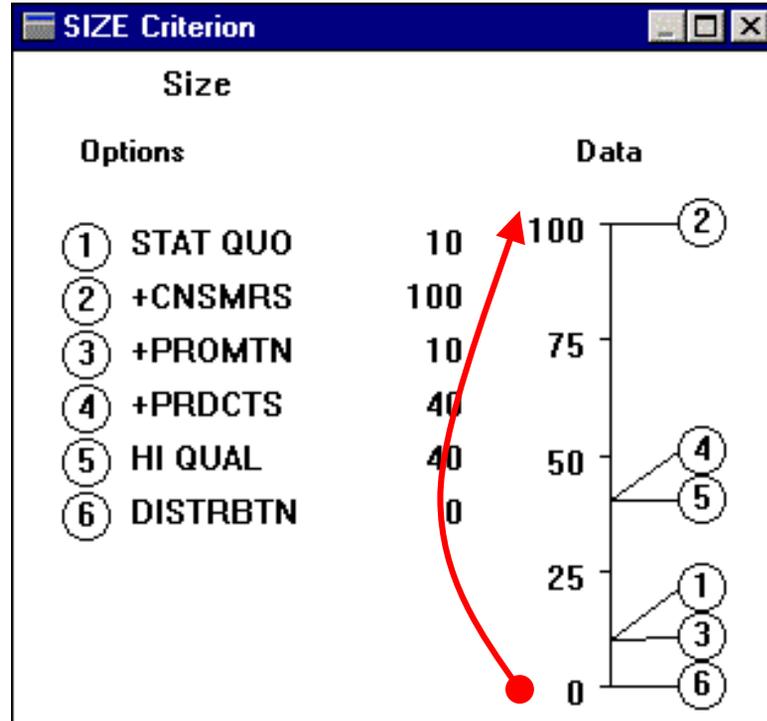
	C1	C2	C3	C4	C5	C6
	PHISICAL	CULTURAL	DELAY IN	TENANT	ACTION	PL. ACTION
	INJURIES	VALUES	ACTION	MOTIVATION	AREAS	AREAS
BEST						
PLAUSIBLE	IMINENT	CLASSIFIED	20	STRONG	ALL THE	IN A PL.
IMPACT	RISK	BUILDING	YEARS	MOTIVATION	BUILDING	AREA
	↑	↑	↑	↑	↑	↑
		OR		OR		OR
WORST						
PLAUSIBLE	ABSENCE	NORMAL	0	NORMAL	ONE	OUT OF
IMPACT	OF RISK	BUILDING	YEARS	MOTIVATION	FLAT	PL. AREA

	C6	C1	C5	C2	C4	C3
	IN A PL. AREAS	IMINENT RISK	ALL THE BUILDING	CLASSIFIED BUILDING	STRONG MOTIVATION	
100						20 YEARS
	OUT OF PL. AREAS	ABSENCE OF RISK	ONE FLAT	NORMAL BUILDING	NORMAL MOTIVATION	0 YEARS
%	100	90	70	50	50	30
Swing						
weights	0,256	0,231	0,18	0,128	0,128	0,077

MACBETH weighting procedure



The difference in attractiveness between this swing and...



...this swing, is:

- very weak
- weak
- moderate
- strong
- v. strong
- extreme

Macbeth : C:\Macbeth\multi\OFF_dom.mcb

File Actions Points of view Windows Options

125% bold Evaluation copy

Points of view

OFFICE

- Turnover
 - Closeness to clients
 - Visibility
 - Image
- Working Conditions
 - Size
 - Comfort
 - Car parking

OFFICE : judgements

	R-close	R-visib	R-comf	R-size	R-image	R-park	Neutral	Current score
R-close	no	weak	moderate	moderate	moderate	strong	positive	33.33
R-visib		no	weak	weak	moderate	moderate	positive	24.24
R-comf			no	weak	weak	moderate	positive	18.18
R-size				no	very weak	weak	positive	12.12
R-image					no	weak	positive	9.09
R-park						no	positive	3.03
Neutral							no	0.00

Consistent judgements

OFFICE : histogram

2) to compare the difference in overall attractiveness between any two swings with the first one is more attractive than the second one

The **tradeoff procedure** has the strongest theoretical foundation (Keeney and Raiffa, 1976). The key idea is to compare two options described on two criteria (for the remaining criteria both options have identical impacts). One option has the best impact on the first and the worst impact on the second criterion, the other has the worst on the first and the best on the second criterion. By choosing the preferred option out of the two the decision-maker decides on the “more important” criterion.

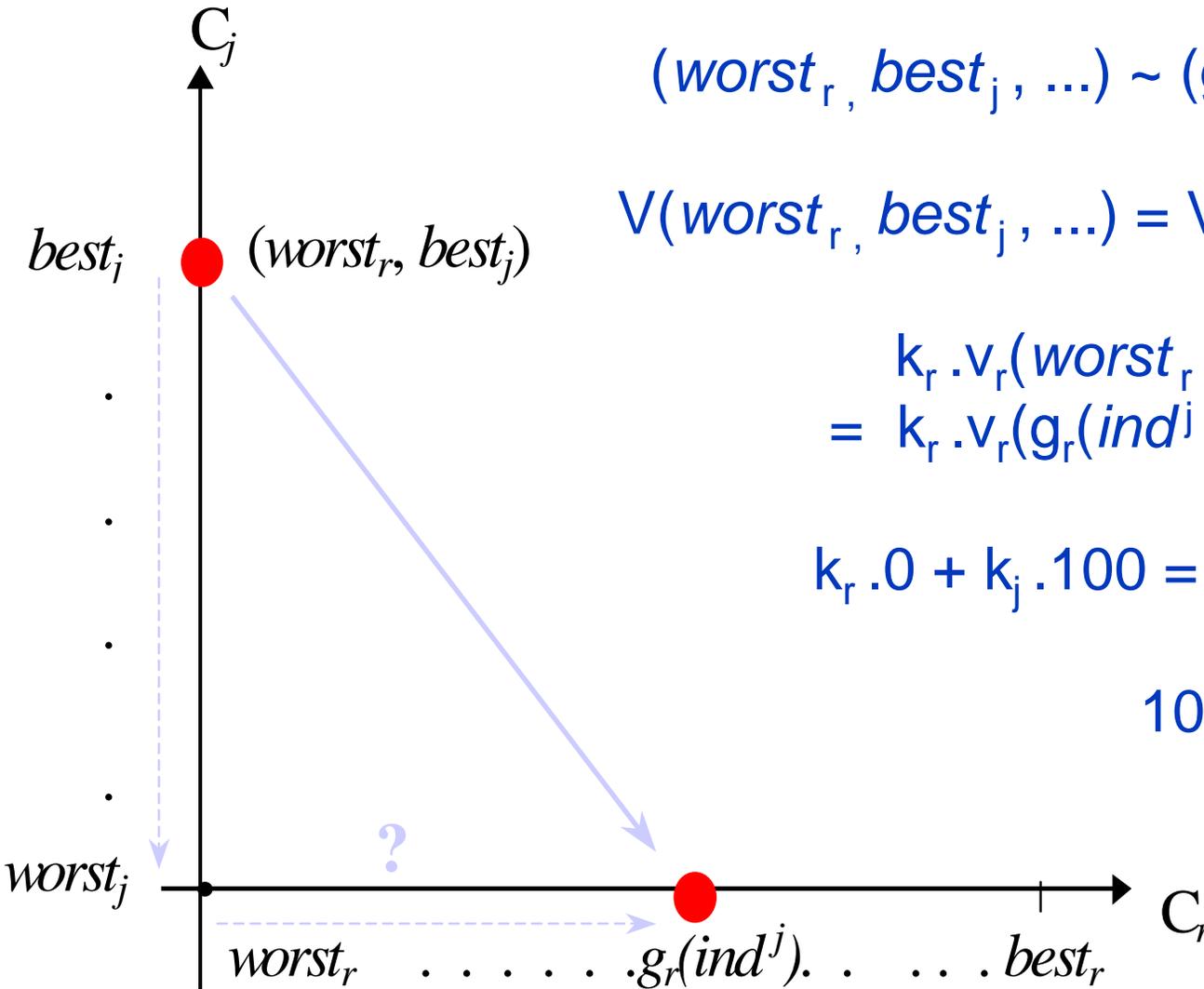
The critical step is the adjustment of the impact level in order to yield indifference between the two options. This is typically done by either worsening the chosen option in the best impact or improving the non-chosen option in the worst impact.

Such differences have to be elicited for the $n - 1$ meaningfully selected pairs of options. If the local value functions are known, numerical values for the scaling constants can be derived.

(Weber & Borcherding, 1993)

Tradeoff procedure

C_r - reference criterion
 C_j - other criteria ($j \neq r$)



$$(worst_r, best_j, \dots) \sim (g_r(ind^j), worst_j, \dots)$$

$$V(worst_r, best_j, \dots) = V(g_r(ind^j), worst_j, \dots)$$

$$k_r \cdot v_r(worst_r) + k_j \cdot v_j(best_j) + \dots = k_r \cdot v_r(g_r(ind^j)) + k_j \cdot v_j(worst_j) + \dots$$

$$k_r \cdot 0 + k_j \cdot 100 = k_r \cdot v_r(g_r(ind^j)) + k_j \cdot 0$$

$$100 k_j = k_r \cdot v_r(g_r(ind^j))$$

SENSITIVITY ANALYSIS ON THE WEIGHTS

$V(a, x_j)$

